



Grantham Research Institute on  
Climate Change and  
the Environment



# **ADAPTATION TO CLIMATE CHANGE AND ECONOMIC GROWTH IN DEVELOPING COUNTRIES**

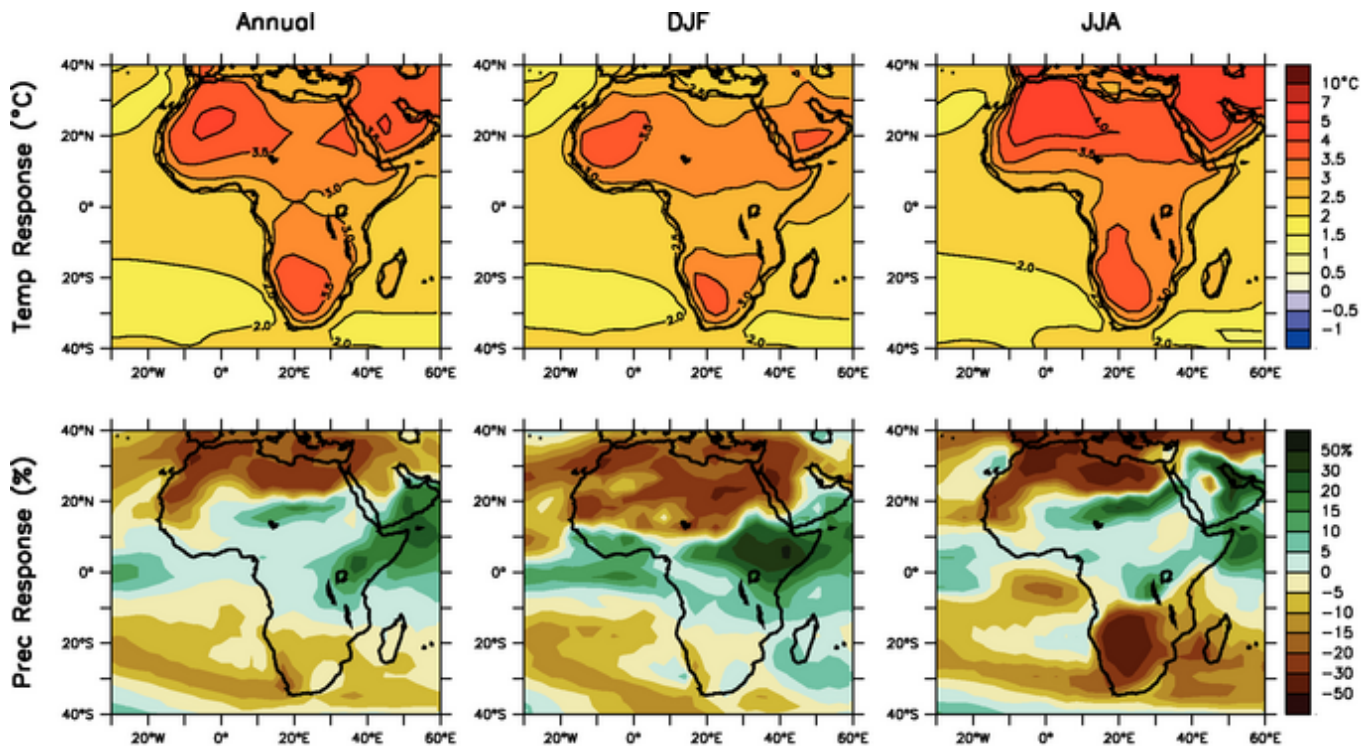
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# STYLIZED FACTS

Developing countries, particularly in sub-Saharan Africa, are highly vulnerable to climate change:

- Geographic location
- High sensitivity (e.g. share of GDP in agriculture)
- Low adaptive capacity (e.g. finance, institutions, information)



Even if (and that's a BIG "if") we get effective mitigation, climate change will occur due to long residence time of atmospheric CO<sub>2</sub>.

# THIS PAPER IN A NUTSHELL

## How should developing countries adapt to climate change?

- “Development is the best form of adaptation” – i.e. invest as usual in productive capital
- “Development is contingent on adaptation” – i.e. invest to ‘climate-proof’ productive capital

## Towards adjudicating between these positions, we:

- Construct a fully dynamic, easy to interpret, analytical model of adaptation as an investment problem at the macro level
- Apply the model empirically to Sub-Saharan Africa, with extensive sensitivity analysis

**We find that in most contingencies it will be optimal to grow the stock of adaptive capital rapidly over the next 50 years.**

# MODEL SETUP

## Modified Ramsey-Cass-Koopmans growth model (cf. DICE)

### Two capital stocks

- ‘Vulnerable capital’ – productive, but damaged by CC
- ‘Adaptive capital’ – unproductive in the absence of CC, but reduces CC damages to vulnerable capital output

### Two controls

- Consumption/investment in vulnerable capital
- Investment in adaptive capital

### Exogenous temperature change (small developing country/region), population and TFP

### Convex cost of investment in adaptive capital

Captures barriers to adapting quickly such as planning costs, policy delays and corruption

# MODEL SETUP II

**Social Planner's Objective:**  $\max_{c(t), I(t)} \int_0^T L(t)U(c(t))e^{-\rho t} dt$

**Vulnerable capital  $K_V$ :**

$$\dot{K}_V = A(t)D(K_A, X(t))F(K_V, L(t)) - \delta_V K_V - cL(t) - Q(I)$$

TFP  $\nearrow$   $A(t)$     Damages =  $D(\text{Adaptive capital}, \text{Exogenous Temperature})$   $\nearrow$   $D(K_A, X(t))$     GDP  $\downarrow$   $F(K_V, L(t))$     Depreciation  $\downarrow$   $\delta_V K_V$     Adaptation costs  $\searrow$   $cL(t)$     Consumption  $\nwarrow$   $cL(t)$      $Q(I)$

**Adaptive capital  $K_A$ :**


$$\dot{K}_A = I - \delta_A K_A$$

Adaptive investment  $\uparrow$   $I$     Depreciation  $\nwarrow$   $\delta_A K_A$

# INTERACTION BETWEEN ADAPTIVE CAPITAL AND CLIMATE CHANGE

All interactions are captured by the modified damage multiplier:

$$D(K_A, X) : \mathbb{R}^+ \times \mathbb{R}^+ \rightarrow [0, 1]$$

  
Adaptive capital      Temperature

We assume:

1.  $D$  is decreasing in  $X$  (climate change is ‘bad’).
2.  $K_A$  unproductive in the absence of climate change (i.e.  $D(K_A, 0) = 1$ )
3.  $D$  is increasing and concave in  $K_A$ .
4. “Productivity” of the marginal unit of  $K_A$  is increasing in  $X$ , i.e.  $\frac{\partial^2 D}{\partial K_A \partial X} > 0$

# MODEL EQUATIONS

## State equations:

$$\dot{K}_V = A(t)D(K_A, X(t))F(K_V, L(t)) - \delta_V K_V - cL(t) - Q(I)$$

$$\dot{K}_A = I - \delta_A K_A$$

## Euler equations (follow from Maximum principle):

$$\dot{c} = \frac{c}{\eta(c)} [A(t)D(K_A, X(t))F_{K_V} - \delta_V - \rho] \quad \leftarrow \text{Ramsey eq}^n$$

$$\dot{I} = \frac{Q'(I)}{Q''(I)} [A(t)D(K_A, X(t))F_{K_V} - \delta_V + \delta_A] - \frac{1}{Q''(I)} A(t)D_a(K_A, X(t))F(K_V, L(t))$$



**Capital adjustment eq<sup>n</sup>:** Make marginal products of  $K_A$  &  $K_V$  more equal, but not “too fast”.

**Terminal conditions:** Pick values for  $K_V(T)$ ,  $K_A(T)$

4 dimensional coupled nonlinear system.

We are interested in the **transient** (not steady state) regime

# DEPENDENCE OF OPTIMAL INVESTMENT RULE ON CAPITAL (NO ADJUSTMENT COSTS)

For simplicity, assume:

- $Q(I) = I$ , i.e. no adjustment costs.
- Depreciation rates of two types of capital are equal.

$$I = R_X(K_V, K_A, X)\dot{X} + R_V(K_V, K_A, X)\dot{K}_V + \delta_A K_A$$

**Remark:** If  $\dot{X} > 0$  and  $\dot{K}_V > 0$ , then  $I > 0$  (since  $R_V > 0$  and  $R_X > 0$ )

**Proposition:**

$R_X$  is an increasing (decreasing) function of  $K_V$  when  $\epsilon_{a,a} < \epsilon_{X,a}$  ( $\epsilon_{a,a} > \epsilon_{X,a}$ )  
 $R_V$  is decreasing in  $K_V$

**Implications:**

- The strong “adapt through development” position is probably not optimal.
- Richer economies respond proportionately less to changes in  $K_V$  but may respond proportionately *more* to changes in  $X$  if the damage reduction effect of a marginal unit of adaptive capital outweighs its effect on the returns to adaptive investment.



# FULL DYNAMIC SIMULATIONS FOR SUB-SAHARAN AFRICA

## Why Sub-Saharan Africa?

- Small emitter of carbon: reasonable to assume climate change is exogenous
- Highly vulnerable to climate change

## Close the model:

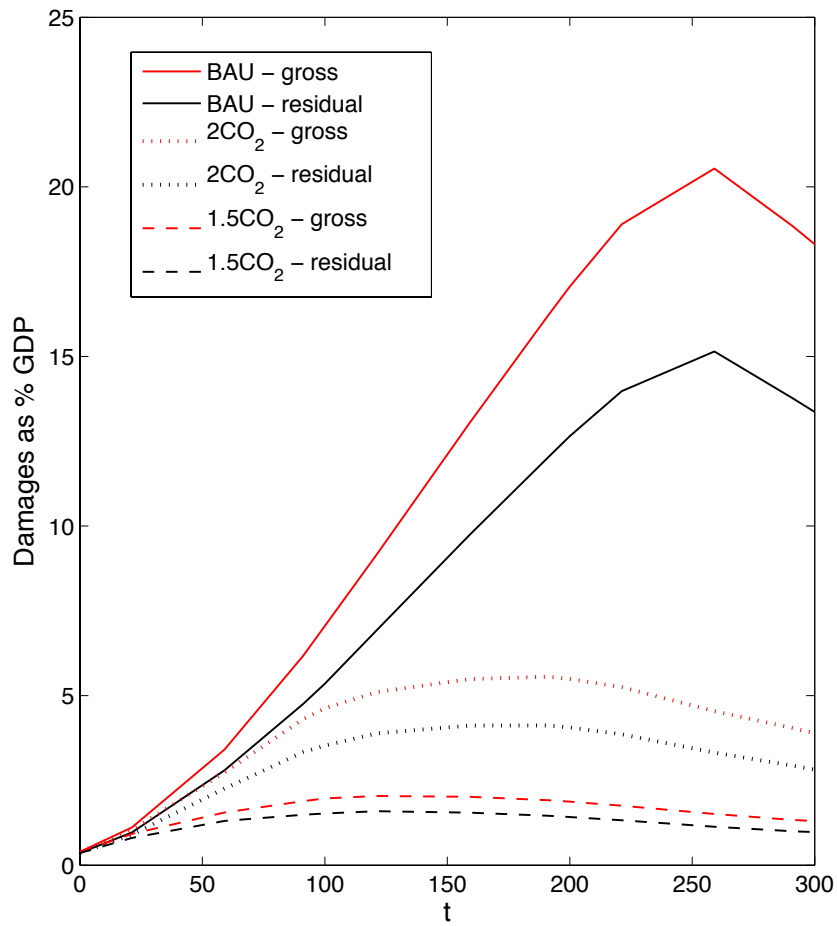
- Choose sensible functional forms for:  
 $D(K_A, X)$ ,  $F(K_V, L)$ ,  $Q(I)$  and  $U(c)$
- Calibrate model parameters based on IAM literature

## Note calibration takes into account:

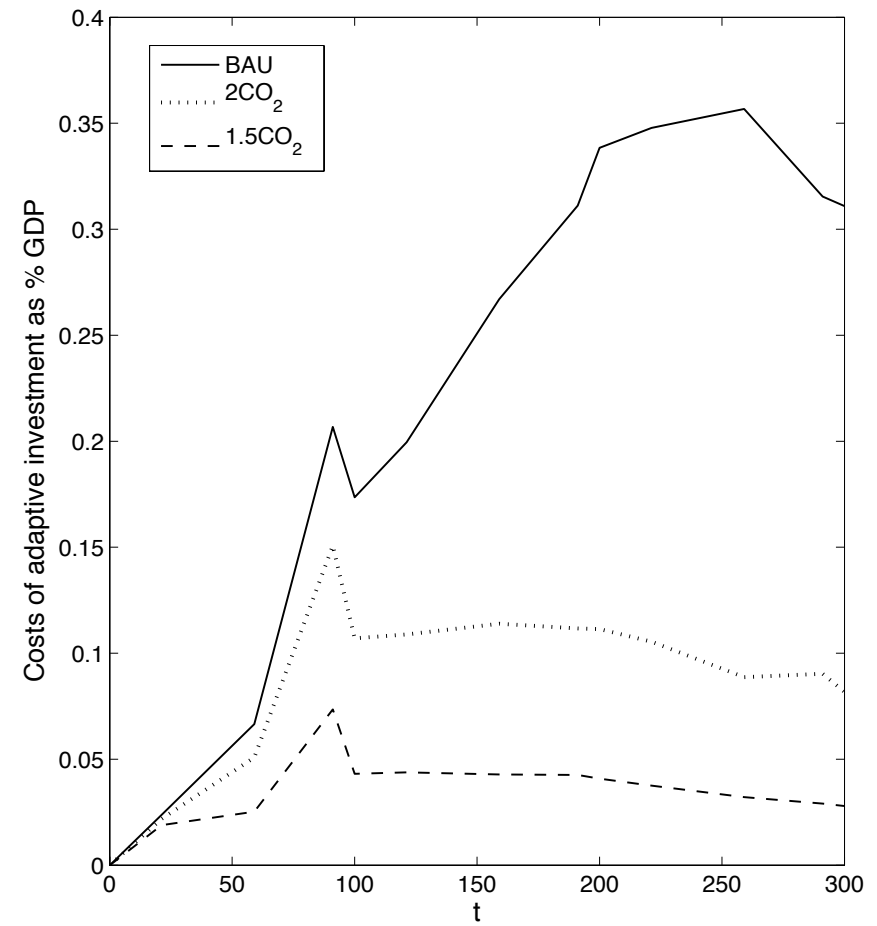
1. Flow adaptation
2. Relationship between income and damages

# BASE CASE : COSTS & BENEFITS

## Damages as % GDP



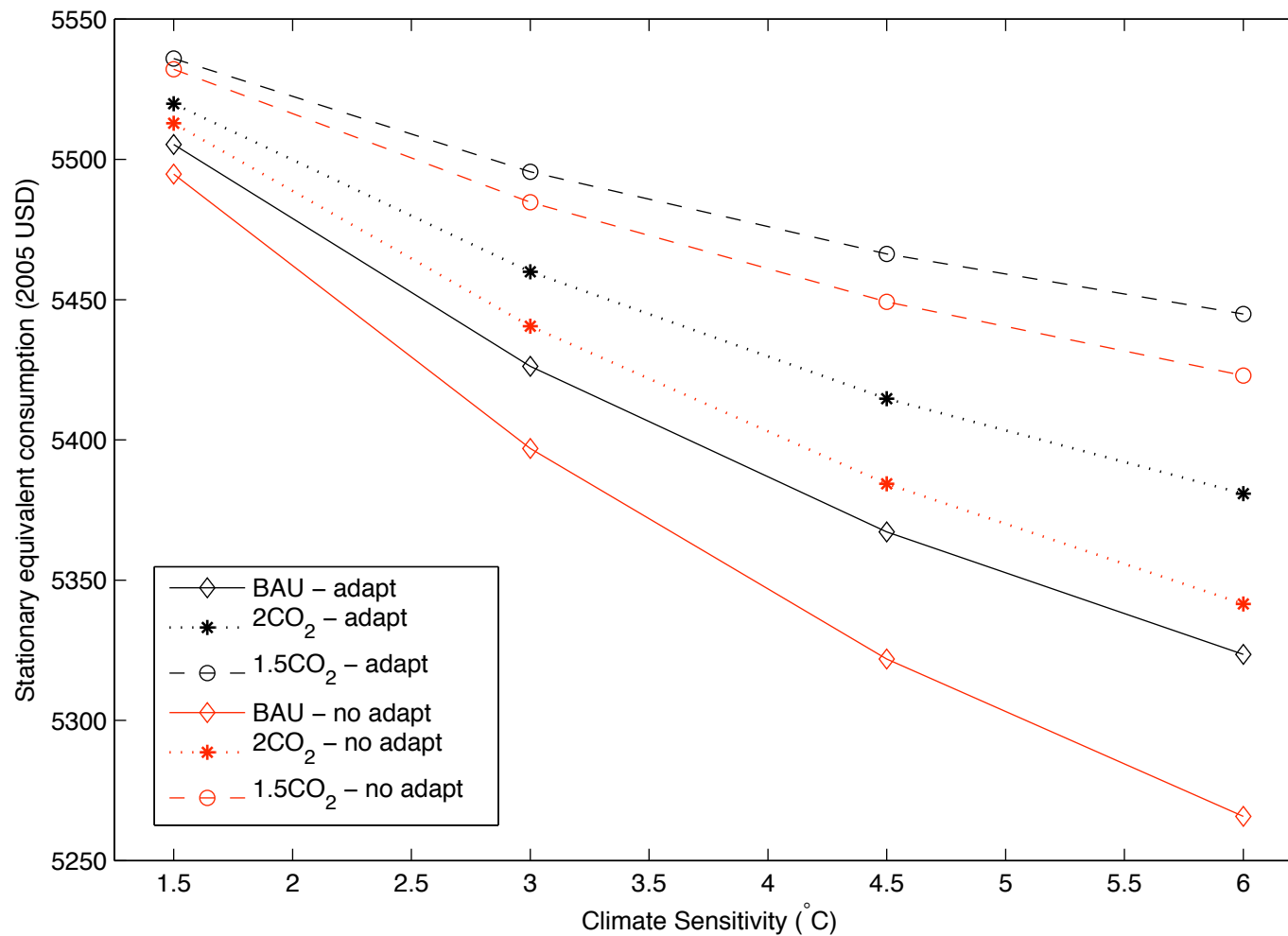
## Investment Costs as % GDP



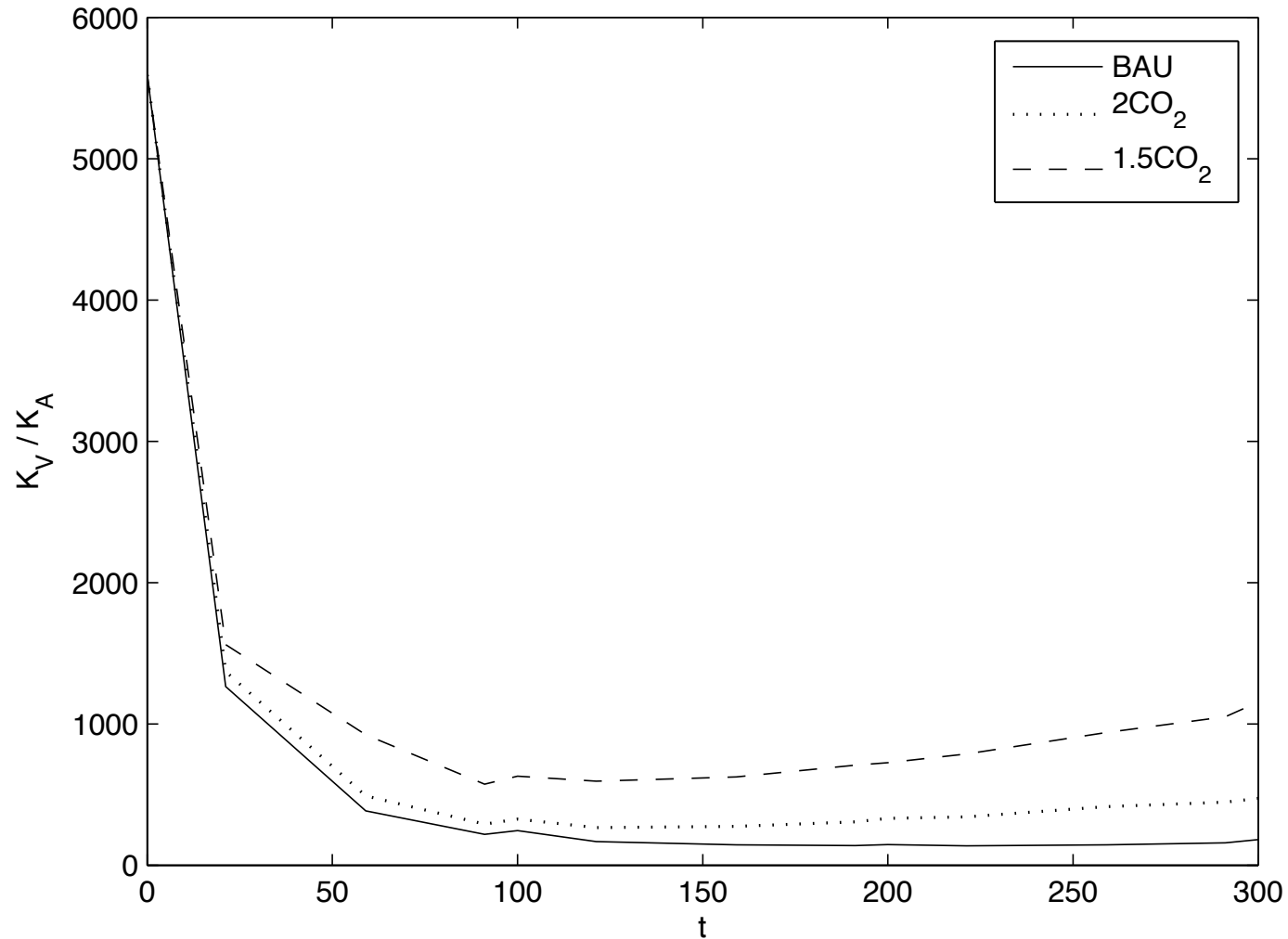
Same order of magnitude as AD-WITCH model.

# WELFARE VS. CLIMATE SENSITIVITY

## WITH AND WITHOUT ADAPTATION



# BASE CASE: RATIO OF VULNERABLE TO ADAPTIVE CAPITAL AS FUNCTION OF TIME (BOTH CHOSEN OPTIMALLY)



# **ROBUSTNESS OF CAPITAL RATIO TRAJECTORY**

**The qualitative ‘U-shaped’ dependence of the capital ratio on time is robust to plausible changes in the values of:**

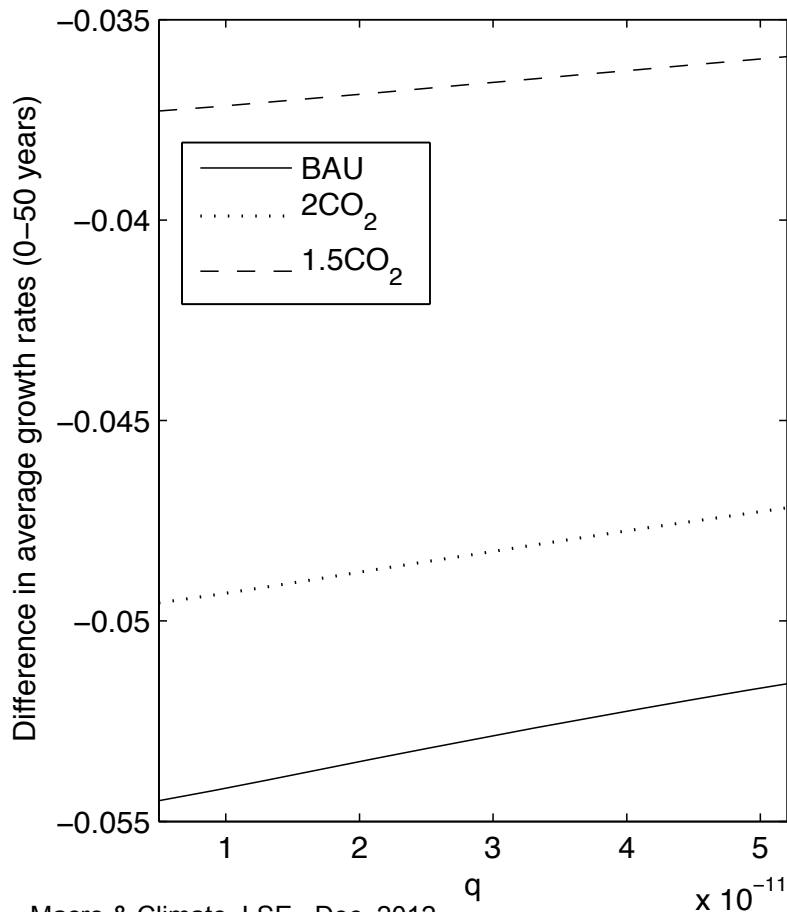
- 1. Adjustment cost parameter**
- 2. Rate of growth of TFP**
- 3. Pure rate of time preference**
- 4. Elasticity of Marginal Utility**
- 5. Climate sensitivity and emissions pathway**

**It is NOT robust to changes in:**

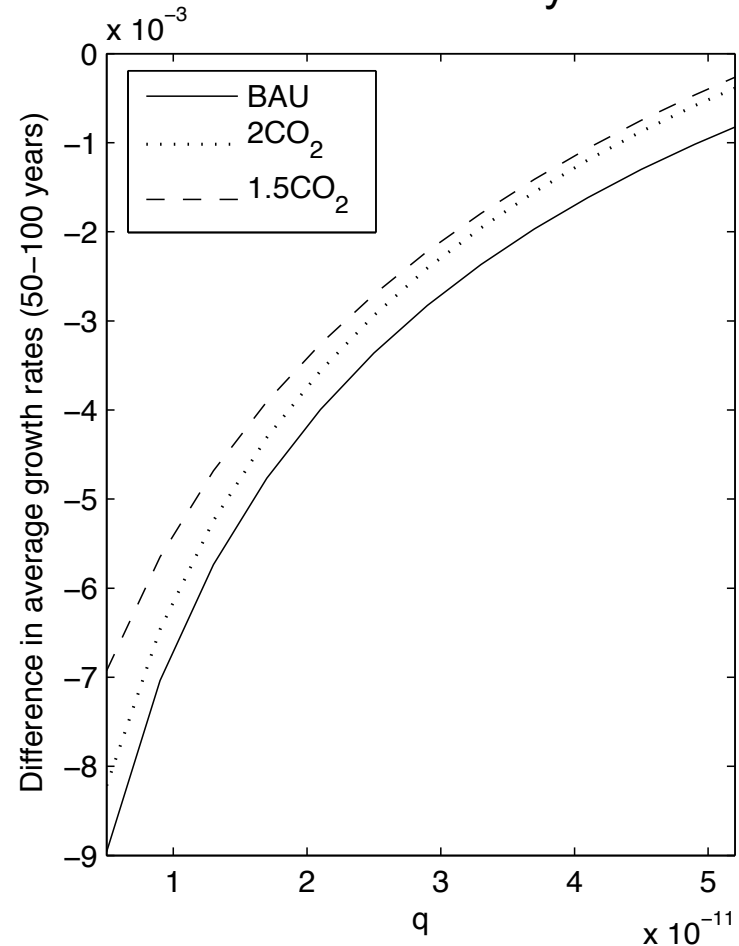
- 1. An ‘Adaptation Effectiveness’ parameter**
- 2. Initial stock of adaptive capital**

# SENSITIVITY TO ADJUSTMENT COSTS: DIFFERENCE IN GROWTH RATES OF VULNERABLE AND ADAPTIVE CAPITAL VS. ADJUSTMENT COST PARAMETER

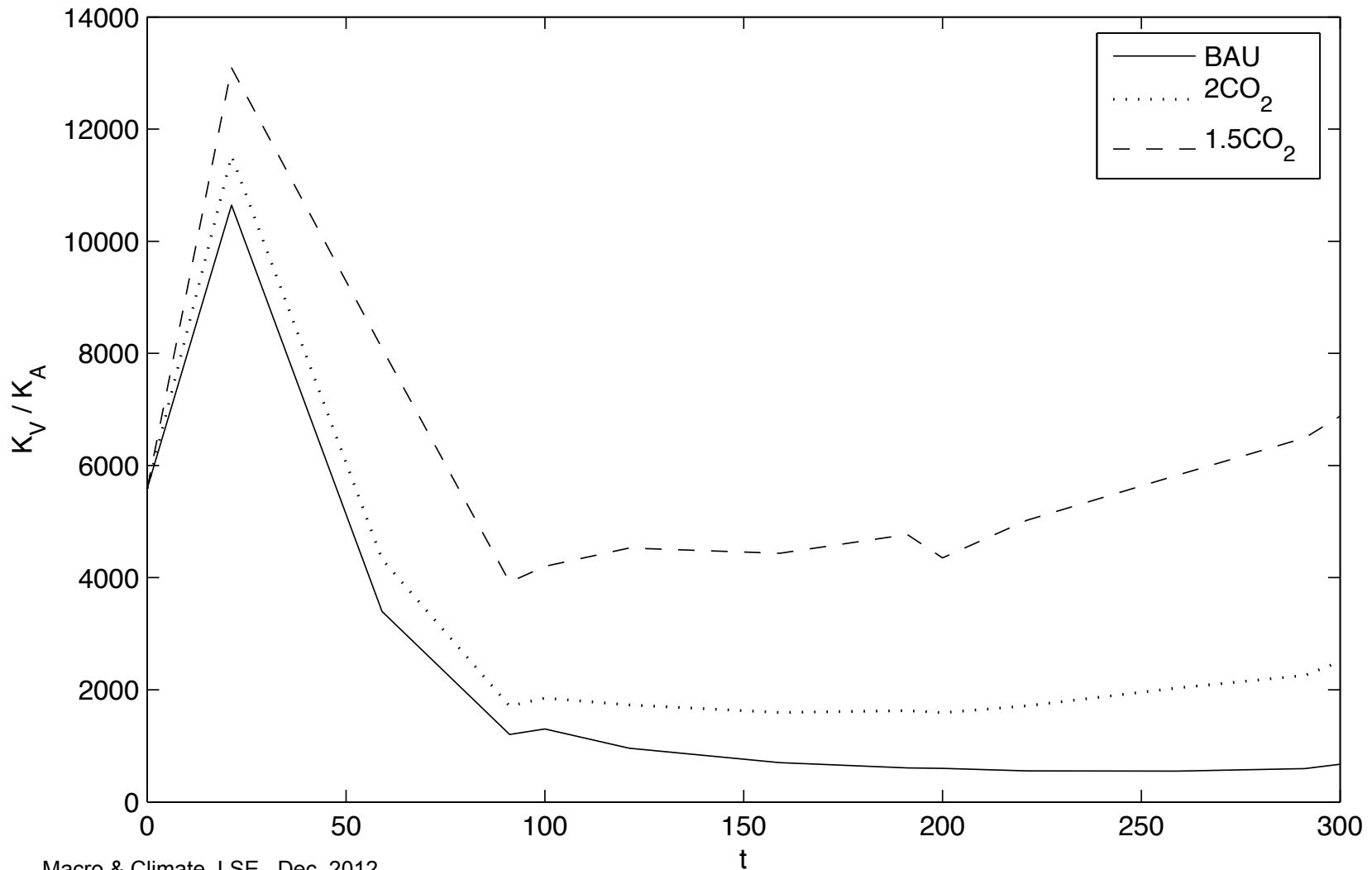
First 50 years



Second 50 years

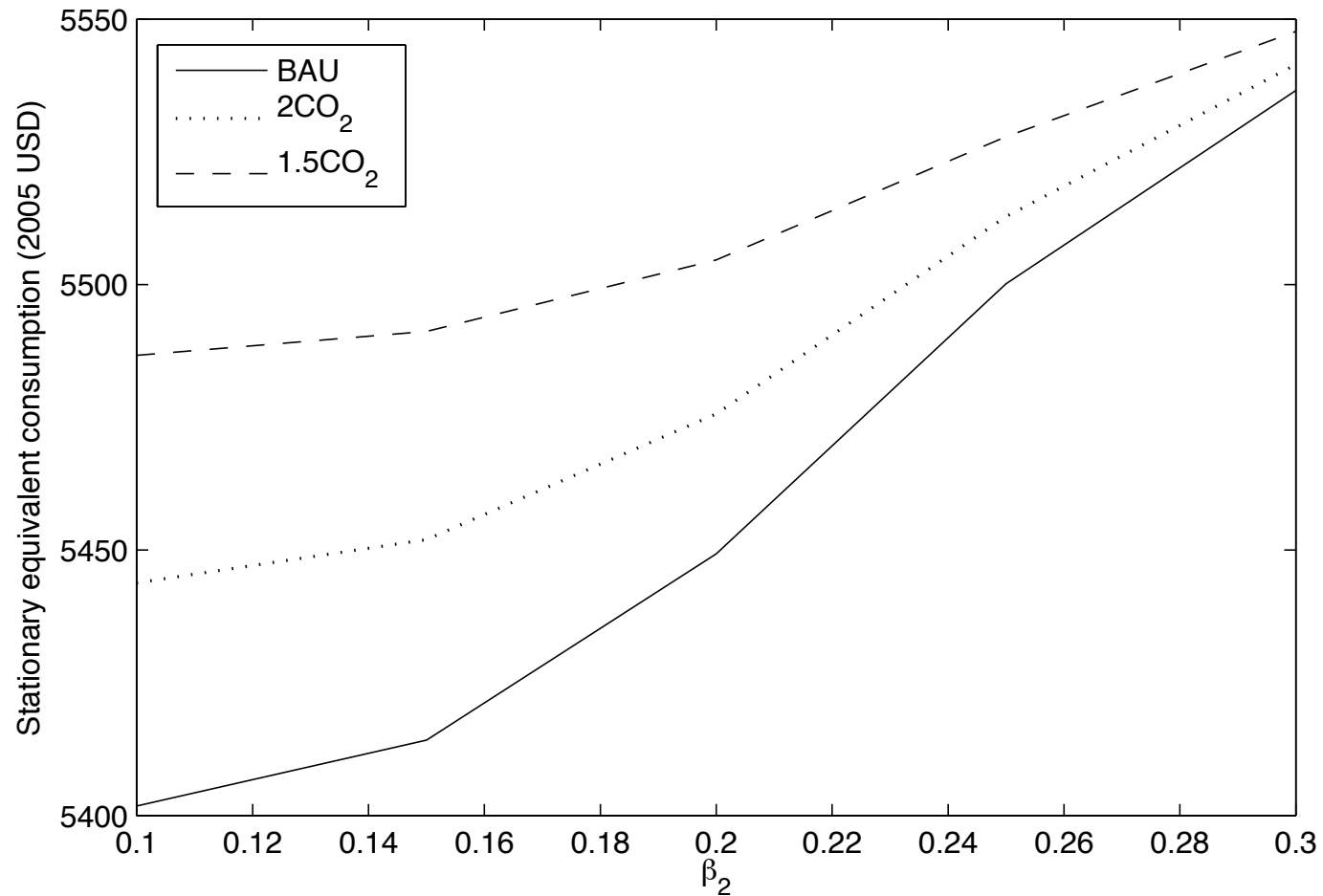


# CAPITAL RATIO FOR LOW ADAPTATION EFFECTIVENESS



# SENSITIVITY TO ADAPTATION EFFECTIVENESS

## WELFARE VS. ADAPTATION EFFECTIVENESS PARAMETER





# CONCLUSIONS

**Developed a simple, transparent model for informing policy discussions.**

**In most plausible cases, we find that it is optimal to grow the stock of adaptive capital rapidly over the next 50 years.**

**This conclusion is robust to changes in the values of all model parameters, *except*:**

- i) Effectiveness of adaptation
- ii) Initial stock of adaptive capital (which is probably very low)

**These are the parameters we should focus on pinning down empirically.**

**Our analytics show that simple *ad hoc* prescriptions are almost certainly wrong: Everything depends on empirical details.**

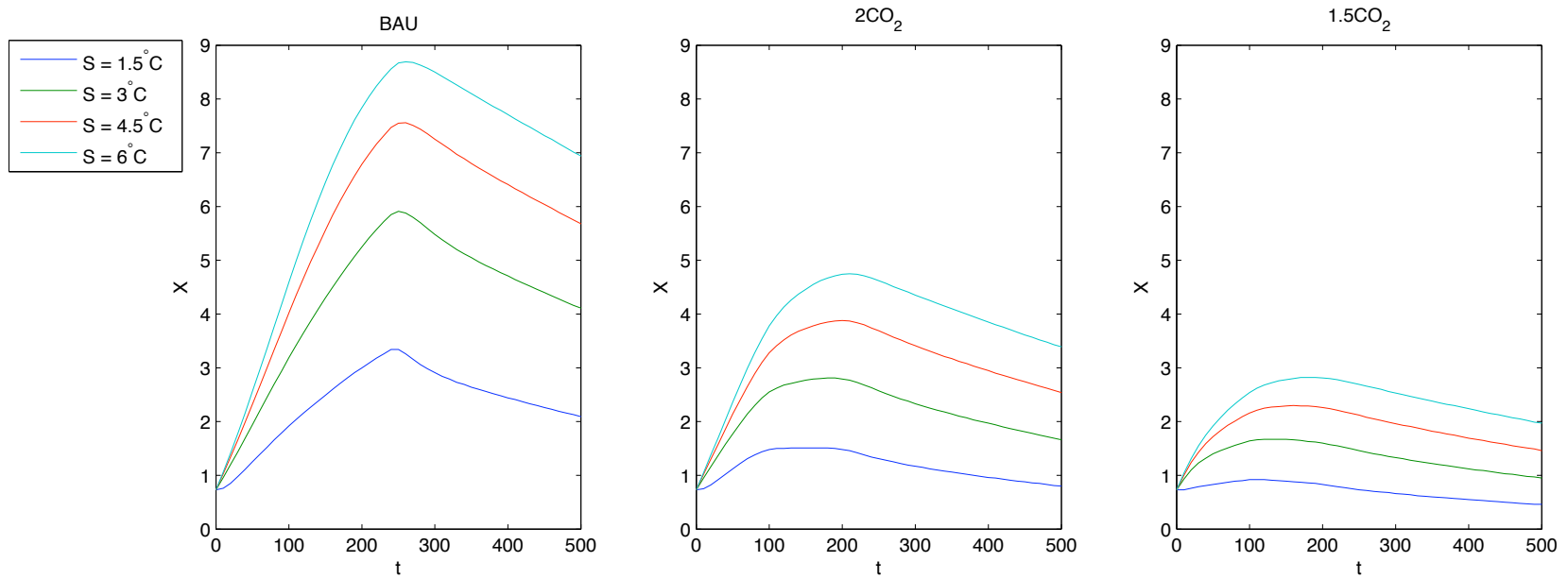
**Caveats: Uncertainty & Learning, Thresholds, Extreme Events, Institutions, etc., etc.**

# **ADDITIONAL MATERIALS**

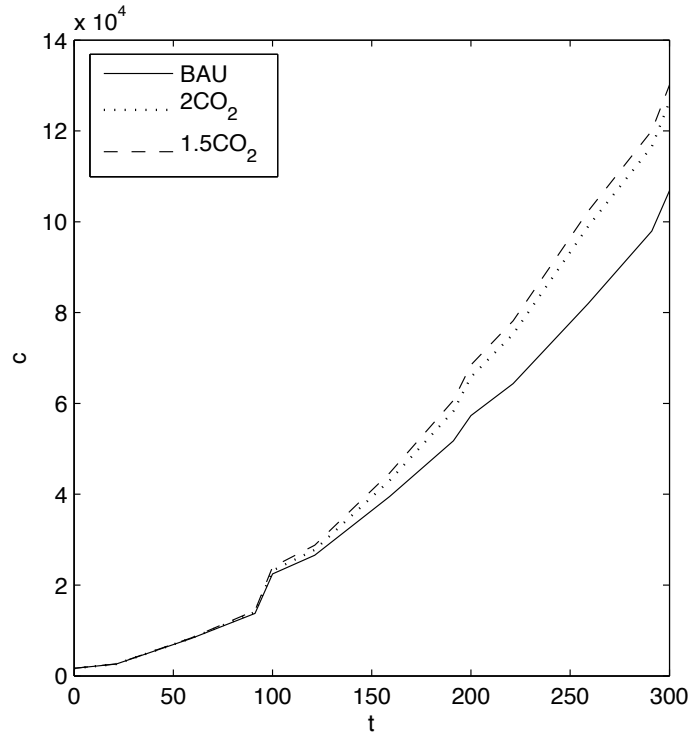
# MODEL PARAMETERS – BASE CASE CALIBRATION

Parameter	Interpretation	Base case value
$\gamma$	Capital share of production	0.3
$\alpha_1, \alpha_2$	Gross damage multiplier parameters	$(2.22 \times 10^{-14}, 0.75 \times 10^{-14})$
$\beta_1, \beta_2^*$	Residual damage multiplier parameters (effectiveness of adaptation)	$(0.32 \times 10^{-2}, 0.17)$
$\delta_A, \delta_V$	Capital depreciation rates	10%/year
$q^*$	Cost of adjustment parameter	$9.70 \times 10^{-12}$
$\eta^*$	Elasticity of marginal utility	2
$\rho^*$	Rate of pure time preference	1.5%/year
$L(t)$	Population	From RICE
$A(t)^*$	Total factor productivity	From RICE
$X(t)^*$	Temperature change	From DICE
$K_V(0)/L(0)$	Initial stock of vulnerable capital per capita	\$2796
$K_A(0)/L(0)^*$	Initial stock of adaptive capital per capita	\$0.50

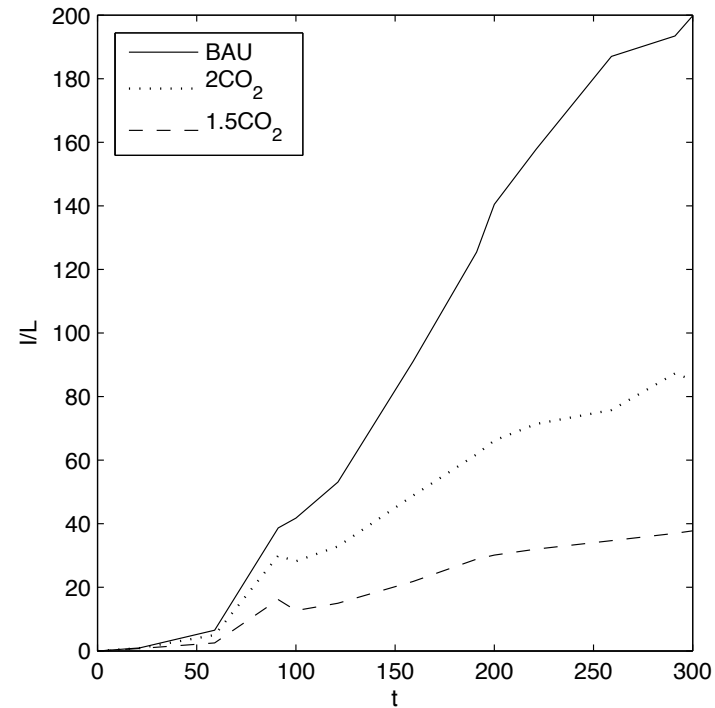
# GLOBAL TEMPERATURE TRAJECTORIES



# BASE CASE RESULTS: OPTIMAL CONTROLS

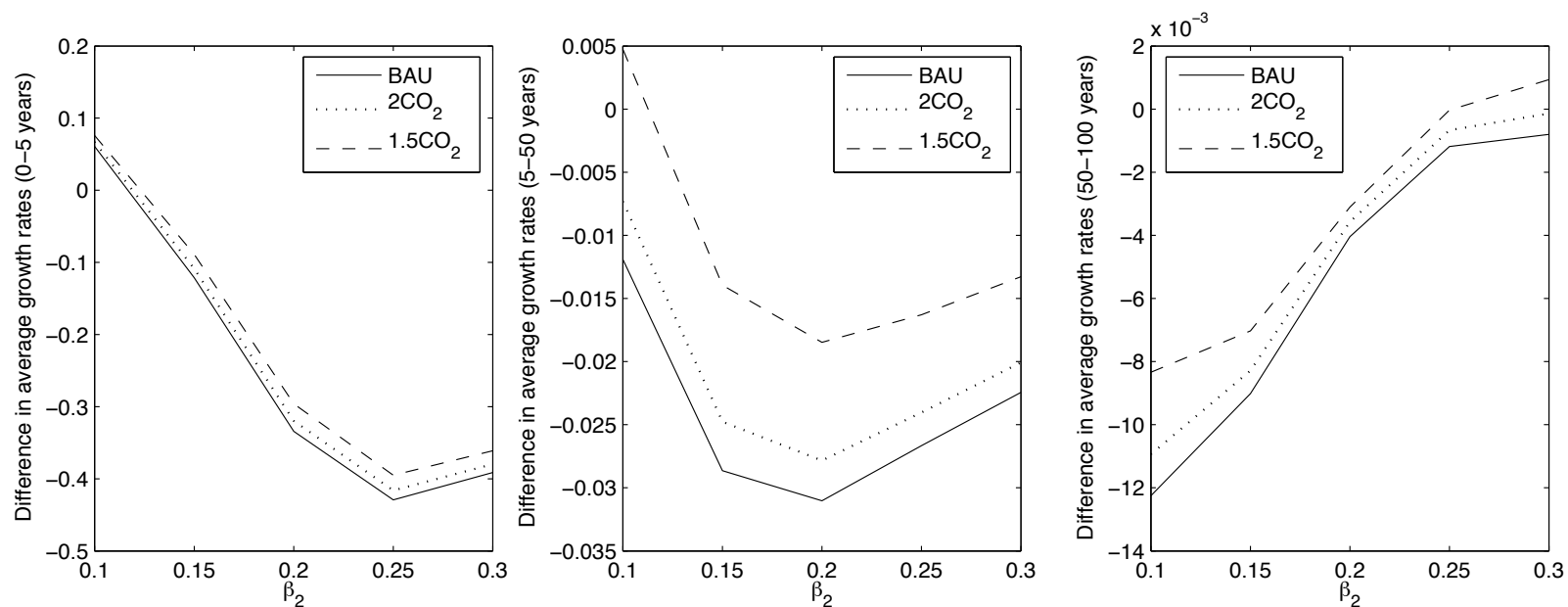


Consumption per capita vs. time



Adaptive investment per capita vs. time

# SENSITIVITY TO ADAPTATION EFFECTIVENESS: ( $G_V - G_A$ )



# SENSITIVITY TO DISCOUNT RATE: RATE: CAPITAL RATIO

