# The Role of Electricity Investments in Africa's Growth: A Macroeconomic Analysis

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	1990s	Since 2000
Annualized GDP Growth Rate	2.5	6.0
Countries with GDP Growth $\geq 5\%$	5	16
% of Population in Country w/ Growth $\geq 5\%$	14	66

Countries with 5% annualized growth doubled their GDP since 2000.

### Africa's Growth in Manufacturing and Services Since 2000



• Many potential sources; relative importance not yet well understood

• This paper focuses on role of electricity investments

· Many African countries have made massive investments in electric power

• Hard to imagine robust non-agricultural growth without electricity

### Africa's Electricity Growth Since 2000



■ GDP ■ Electricity Consumption ■ Electricity Production

## Much of Electricity Growth is Hydropower



Figure: Gilgel Gibe III Dam in Ethiopia

## Much of Electricity Growth is Hydropower

• Hydropower  $\sim$  around 70% of total in Sub-Saharan Africa, excluding South Africa (Eberhard et al, 2011)

• Exceptions like South Africa (coal), Nigeria (gas), Senegal (Oil)

• Enormous future potential, e.g. Inga 3 project at mouth of Congo River

### Correlation with Electricity Growth, 18 SSA countries

	Correlation Coefficient	<i>p</i> -value
GDP growth	0.63	0.007
Manufacturing GDP growth	0.76	0.001
Services GDP growth	0.63	0.008

## This Paper: Quantify Role of Electricity in Africa's Growth

• How much of Africa's growth was caused by electricity investments?

• Challenge: reverse causality: growth increases the demand for electricity, and non-agricultural goods, which use more electricity

• Direct econometric approach - instruments at country level - very hard

## This Paper: Quantify Role of Electricity in Africa's Growth

• Our approach: use "structural" macro approach

• Measure electricity supply increases directly

- Discipline demand side using (known) income elasticities of demand
  - for electricity
  - for non-agricultural goods, which use electricity intensively
  - $\Rightarrow$  Constrains magnitude of "reverse causality" story

- Focus on Africa's 6 largest economies, excluding South Africa, since 2000
- Electricity accounts for  $\sim$  <u>one third</u> of growth in GDP/capita
- Range: 23% to 48% for Nigeria, Ethiopia, Kenya, Tanzania and Sudan; Just 2% in DR Congo
- Quantitative conclusions depend on labor/capital being poor substitutes for electricity in model

### Model

### Households and Preferences

#### Preferences

$$\mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t U(C_{a,t}, C_{n,t}, C_{e,t})$$

where

$$U(C_{a,t}, C_{n,t}, C_{e,t}) = \omega_a \log(C_{a,t} - \bar{a}) + \omega_n \log(C_{n,t}) + \omega_e \log(C_{e,t})$$

- $C_{a,t}$ ,  $C_{n,t}$ ,  $C_{e,t}$ : consumption of agriculture, non-agriculture and electricity
- $-\bar{a}$  is a "subsistence need"; relative demand for  $C_n$  and  $C_e$  rise with income
- follow structural change lit., i.e. Herrendorf, Valentinyi, Rogerson (2014)

Agriculture sector:

$$Y_{a,t} = A_t K_{a,t}^{\theta} N_{a,t}^{1-\theta}$$

Non-agriculture sector:

$$Y_{n,t} = A_t \left[ \mu(K_{n,t}^{\theta} N_{n,t}^{1-\theta})^{\frac{\epsilon-1}{\epsilon}} + (1-\mu) E_{n,t}^{\frac{\epsilon-1}{\epsilon}} \right]^{\frac{\epsilon}{\epsilon-1}}$$

 $-E_{n,t}$  is electric power input

- $\epsilon$  is elasticity of substitution between E and K-N aggregate input
- less substitutability when  $\epsilon \rightarrow 0$
- follows macro-energy literature, e.g. Hassler, Krussell and Olavsson (2015)

#### Production Function

$$E_t = \chi K_{e,t}^{\phi} N_{e,t}^{1-\phi}$$

Electricity capital and labor inputs

- Ke is "electricity capital" e.g. hydroelectric dams, power lines
- Law of motion:  $K_{e,t+1} = K_{e,t}(1-\delta) + I_{e,t}$
- $-I_{e,t}$  financed through taxation, chosen by government
- $N_{e,t}$  hired competitively in labor market
- Resource contraint:  $E_t = E_{n,t} + C_{e,t}$

Budget constraint

$$C_{n,t} + p_{a,t}C_{a,t} + p_{e,t}C_{e,t} + I_t \leq w_t + r_tK_t + \Pi_{e,t} - T_t$$

where

-  $w_t$  is labor income,  $r_t K_t$  is capital income

 $- \prod_{e,t}$  is profits from electricity sector

 $-T_t$  is tax bill (equal to  $I_{e,t}$ )

- Law of Motion for (non-energy) capital:  $K_{t+1} = K_t(1-\delta) + I_t$ 

- Two exogenous sources of growth in model
  - 1. Increases in total-factor productivity,  $A_t$
  - 2. Investments in electricity,  $I_{e,t}$

• Both also lead endogenously to more private investment/capital,  $K_t$ 

• Through lens of model, all GDP per capita growth ultimately due to *I*<sub>*e*,*t*</sub> increases (which we measure directly), or *A*<sub>*t*</sub> increases (the residual)

### Quantifying Sources of Growth using Model

- Focus on two steady states of model: "before 2000" and "after 2000"
- Calibrate model to Ethiopia before 2000; match agriculture employment share (73%), energy investments/GDP (1%), GDP per capita (\$621), electricity per capita (21 kwh / capita)
- Pick  $\epsilon = 0.4$ , following Krusell, Hassler, Olavsson (2015)
- Increase electricity investments, *I<sub>e,t</sub>* to match electricity growth since 2000; increase total-factor productivity, *A<sub>t</sub>*, to match GDP per capita growth
- Repeat for Nigeria, Kenya, DR Congo, Tanzania and Sudan

### Quantitative Results: Growth of GDP per Capita



- Model, Electricity Investments Only
- Fraction Explained

## Preliminary Conclusions and Future Work

• Africa since 2000: high GDP/capita growth & large electricity investments

• Structural macro model: electricity investments explain  $\sim$  one third of growth in six large African countries

· Conclusions depend on electricity and other inputs being poor substitutes

• Future work: better identification of elasticity of substitution; solve full transition; add other African countries; internal evidence from Ethiopia

### **Extra Slides**

## Growth Strongly Correlated with Change in Electricity



## Decomposing Growth Since 2000 Using Model

- First compute steady state with fixed levels of  $\{A_a, A_n, I_e\}$
- Do so by calibrating to match levels in 1990
- Then compute steady state with higher levels  $\{A'_a, A'_n, I'_e\}$
- Pick values of  $\{A'_a, A'_n, I'_e\}$  to match data in 2016
- Model matches all growth by construction
- Decompose growth into three sources; ask what fraction due to electricity

– Pick  $\omega_a = 0.02$ ,  $\omega_n = 0.97$  and  $\omega_e = 0.01$  to match U.S. ("long-run") expenditures shares

– Standard macro choices of  $\beta$  = 0.96,  $\delta$  = 0.07, and  $\theta$  = 0.33 to match returns on capital, depreciation and capital income share in GDP

– Pick  $\phi=$  0.99 to get 1% labor income share in electricity VA

- Pick  $\mu = 0.97$  to get 3% VA share of energy in non-agriculture
- Pick  $\epsilon = 0.5$  as benchmark value; sensitivity analysis later
- Pick  $A_n = A_a$  for now and  $A_n = 1$ ,  $\chi = 1$  as normalization on units
- Calibrate  $\bar{a}$  and  $I_e$  to match Ethiopia's 2000 steady state: (1) agriculture employment share of 75%, (2) electricity investment to GDP of 0.5%

### Model's Other Quantitative Predictions

• Model predicts large movements of workers from agriculture to non-agriculture with electricity investments

• Data: movements out of agriculture, but not as large as model

• Likely to be frictions to worker reallocation that are not in model

### **Solution to Model**

Steady State Solution to Model

From steady state Euler Equation

$$r = 1/\beta + \delta - 1 \tag{1}$$

From FOC for  $K_a$ 

$$\frac{K_a}{N_a} = (p_a A_a \theta r^{-1})^{\frac{1}{1-\theta}}$$
<sup>(2)</sup>

From FOC for Na

$$w = p_a A_a \left(\frac{K_a}{N_a}\right)^{\theta} (1-\theta)$$
(3)

From FOC for  $K_n$ 

$$A_{n}\left[\mu(K_{n}^{\theta}N_{n}^{1-\theta})^{\frac{\epsilon-1}{\epsilon}}+(1-\mu)E_{n}^{\frac{\epsilon-1}{\epsilon}}\right]^{\frac{1}{\epsilon-1}}(K_{n}^{\theta}N_{n}^{1-\theta})^{\frac{-1}{\epsilon}}\mu\theta\left(\frac{K_{n}}{N_{n}}\right)^{\theta-1}=r \quad (4)$$

From FOC for K<sub>a</sub>

$$A_{n}\left[\mu(K_{n}^{\theta}N_{n}^{1-\theta})^{\frac{\epsilon-1}{\epsilon}}+(1-\mu)E_{n}^{\frac{\epsilon-1}{\epsilon}}\right]^{\frac{1}{\epsilon-1}}(K_{n}^{\theta}N_{n}^{1-\theta})^{\frac{-1}{\epsilon}}\mu(1-\theta)\left(\frac{K_{n}}{N_{n}}\right)^{\theta}=w$$
 (5)

Ratio of (5) to (4)

$$\frac{1-\theta}{\theta}\frac{K_n}{N_n} = \frac{w}{r} \tag{6}$$

From FOC for E

$$A_n \left[ \mu (K_n^{\theta} N_n^{1-\theta})^{\frac{\epsilon-1}{\epsilon}} + (1-\mu) E_n^{\frac{\epsilon-1}{\epsilon}} \right]^{\frac{1}{\epsilon-1}} E_n^{\frac{-1}{\epsilon}} (1-\mu) = p_e$$
(7)

Instead of (7), ratio of (4) to (7)

$$\frac{(K_n^{\theta}N_n^{1-\theta})^{\frac{-1}{\epsilon}}\mu\theta(\frac{K_n}{N_n})^{\theta-1}}{(1-\mu)E_n^{-1/\epsilon}} = \frac{r}{p_e}$$
(8)

Reshuffling the above

$$N_n = x^{-\epsilon} \left(\frac{K_n}{N_n}\right)^{-\theta} \tag{9}$$

where  $x = (K_n^{\theta} N_n^{1-\theta})^{\frac{-1}{\epsilon}}$ , and can be backed out from (8)

## Steady State Solution to Model

From energy producer's FOC for  $N_e$ 

$$N_e = (\chi p_e (1 - \phi) w^{-1})^{\frac{1}{\phi}} K_e$$
(10)

From energy producer's profit function

$$\Pi_e = p_e E - w N_e \tag{11}$$

Notice that energy producer has profits because has fixed energy capital stock with which to produce

Household FOC for  $C_a$  and  $C_n$ 

$$C_a = \rho_a^{-1} C_n \frac{\omega_a}{\omega_n} + \bar{a} \tag{12}$$

Budget constraint in steady state

$$C_n = \omega_n [w + k(r - \delta) + \Pi_e - T - p_a \bar{a}]$$
(13)

Household FOC for  $C_e$  and  $C_n$ 

$$C_e = \rho_e^{-1} C_n \frac{\omega_e}{\omega_n} \tag{14}$$